A picture containing chart

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Figure.1 – Reproducing the test case.

Figure.1.a (LEFT): Reproduced test case of the Einstein ring from centred, single pixel source; lensed by equations for a planar, transparent, smooth mass distribution. The source image size is () pixels and lensing is completed with parameters: . The domain of reduced coordinates is kept to . The full ring is produced as expected, at the pre-calculated radius (for ) and a plot of the predicted ring is overlaid.

Figure.1.b (RIGHT): Same system scaled to a larger source image. It uses pixels with 1 pixel centre source and all same parameters. The code still clearly reproduces correct, expected behaviour, the ring is still full, is of approximately equal thickness throughout, and lies at the expected radius.

A picture containing background pattern

Description automatically generated

Figure.2 – Generating and lensing a galaxy cluster.

Figure.2.a (LEFT): Generated cluster of 70 galaxies on a pixel image. The flux profile of all galaxies follows: . Galaxies have randomly generated: positions, angles to horizontal, RGB colours , decay constants in range pixels, minor axis in range pixels and major axis ensured to be larger than minor axis in range . For each galaxy, the parameter in the flux profile has been transformed using the standard 2D rotation matrix . The image has been seeded for reproducibility.

Figure.2.b (RIGHT): Lensed image of generated galaxies (from Figure.2.a) with used lensing parameters: and with expanded domain () of reduced coordinates . The image clearly demonstrates the effect of far galaxies being stretched and pushed to further radii. It is also clear that the galaxy (blue) passing through the centre of the lens produces a nearly ideal Einstein ring with expected radius (). Galaxies near the centre can be viewed twice in the lensed image, as expected for objects positioned within the caustic of the lens.